

Homework 2, week 4 (30 points)

1. (5 points)

Write pseudocode for MERGE(A, p, q, r) .

2. (5 points)

Use merge sort to sort an array $A=\{1, 41, 52, 33, 38, 54, 9, 42\}$. Draw a diagram to show the sorting procedure.

3. (10 points)

Use mathematical induction to show that the solution of the recurrence

$$T(N) = \begin{cases} 2; & \text{if } N = 2 \\ 2T(N/2) + N; & \text{if } N = 2^k, k > 1 \end{cases}$$

is $T(N) = N \log N$.

4. (10 points)

For each function $f(n)$ and time t in the following table, determine the largest size n of a problem that can be solved in time t , assuming that the algorithm to solve the problem take $f(n)$ microseconds.

t \ f(n)	1 second	1 minute	1 hour	1 month	1 year	1 century	
$\lg n$							
\sqrt{n}							
n							
$n \lg n$							
n^2							
n^3							
2^n							
$n!$							

Turning in your work

Submit your results (all in one file and name it as Yourname_hw1.doc or Yourname_hw1.pdf, please) to TA Huimin Lu at linuslu6@outlook.com by 10:00 AM on April 2nd, 2018.

Please cut, sign the following paper, and then return it together with a paper copy of your home work to the teacher.

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独立作业承诺：（请选择一个，并签名）

1. 本人，_____，保证本次作业 hw1 由自己独立完成。

签名

时间 年 月 日

或者

2. 本人，_____，保证本次作业 hw1 和_____同学讨论后，由自己独立完成。
讨论内容包括_____

签名 _____，

时间 年 月 日